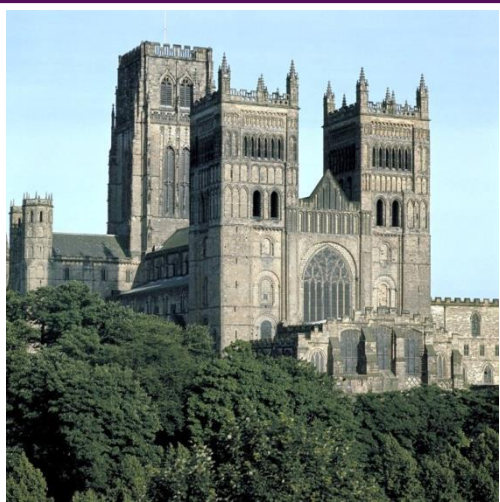


Critical current density in HTS for fusion: TDGL, Experiments, and Irradiation.



Centre for Materials Physics



Durham
University

www.durham.ac.uk/cmp

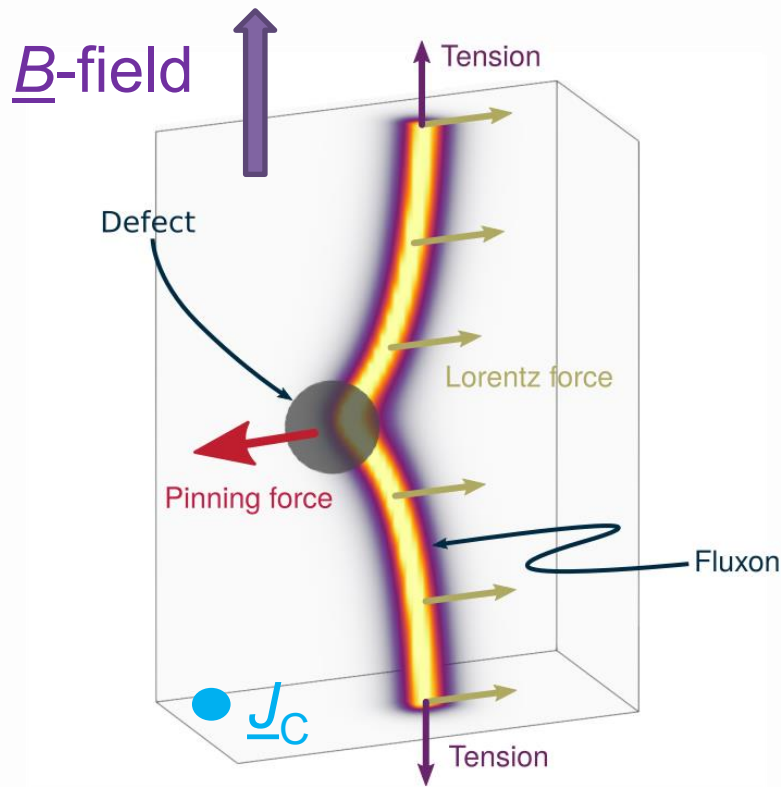
**Prof. Damian P. Hampshire, P. Branch, B. Din,
J. Greenwood, C. Haddon, and M. J. Raine.**

Talk Outline

1. Time-dependent Ginzburg-Landau Theory - Flux pinning visualisation.
2. Critical current experiments on HTS
3. Irradiation
4. Concluding comments.

Flux Pinning (Parametrisation)

- Magnitude of the order parameter



Flux pinning curve scales well with field, temperature and strain

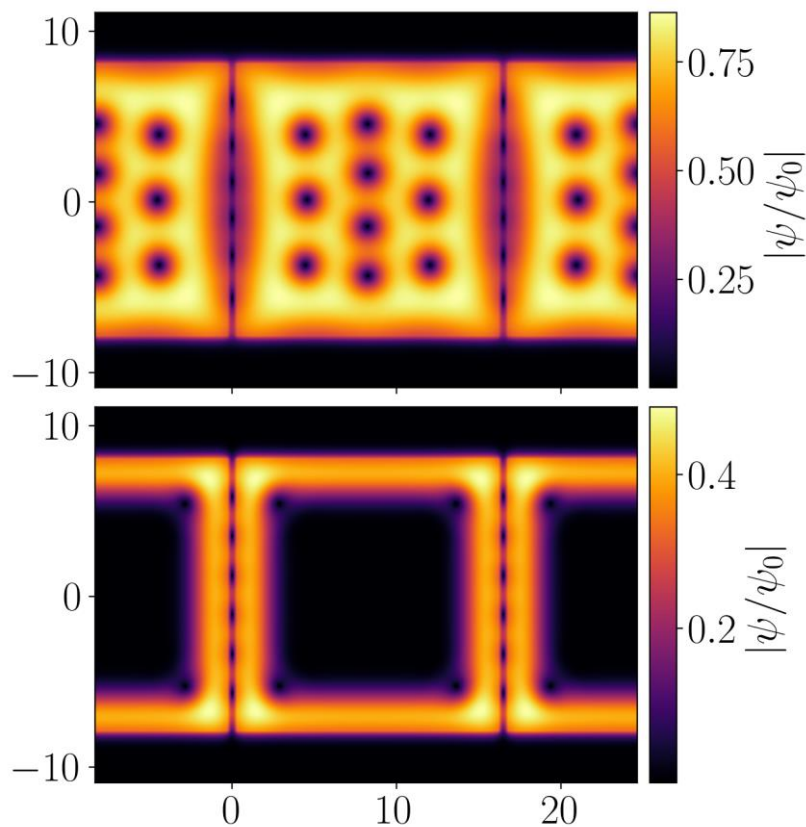
$$F_p = J_c B = C \left(\frac{B}{B_{c2}} \right)^p \left(1 - \frac{B}{B_{c2}} \right)^q$$

$$\underline{F}_V = - \underline{J}_C \times \underline{B}$$

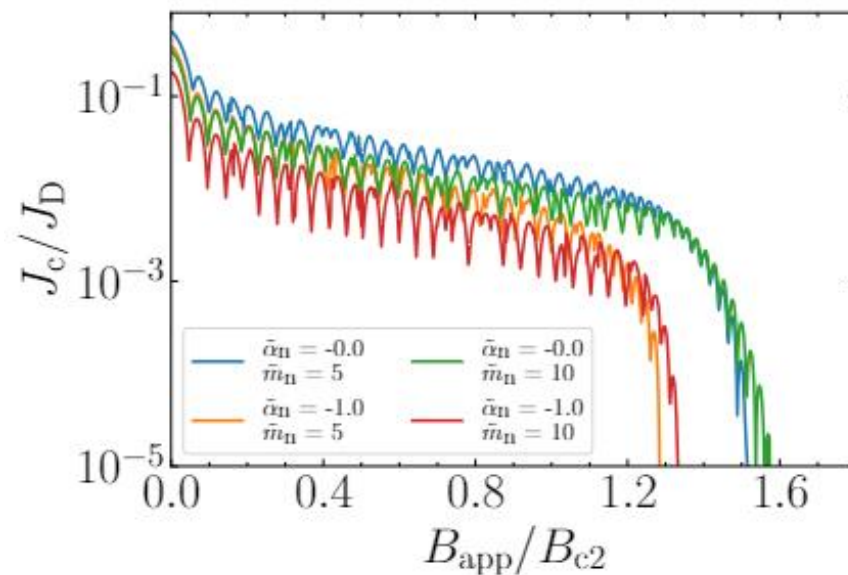
\underline{F}_V : Lorentz Force on fluxon

Josephson junctions

- Phase of the order parameter.



The normalized order parameter magnitude at $B = 0.5 B_{c2}$ (top) and $B = 1.1 B_{c2}$ (bottom) for two SNS junctions.



Critical current density as a function of applied magnetic field for an SNS junction with a range of different junction properties.

Ginzburg-Landau theory

Ginzburg and Landau (G-L) postulated a free energy density functional for superconductors of the form:

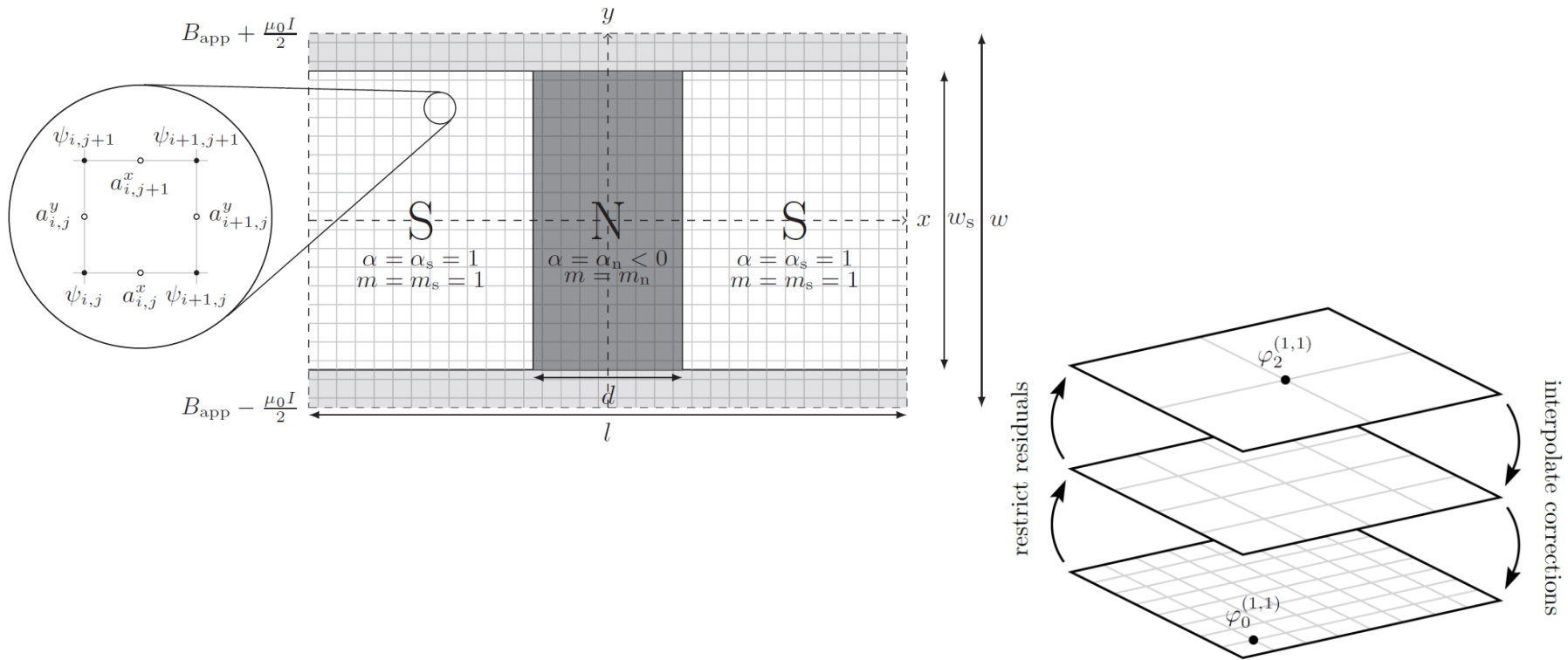
$$f = \alpha |\psi|^2 + \frac{1}{2} \beta |\psi|^4 + \frac{1}{2m} |(-i\hbar\nabla - 2e\mathbf{A})\psi|^2 + \int \mathbf{H}d\mathbf{B}$$

Condensation energy

Kinetic energy

Magnetic field energy

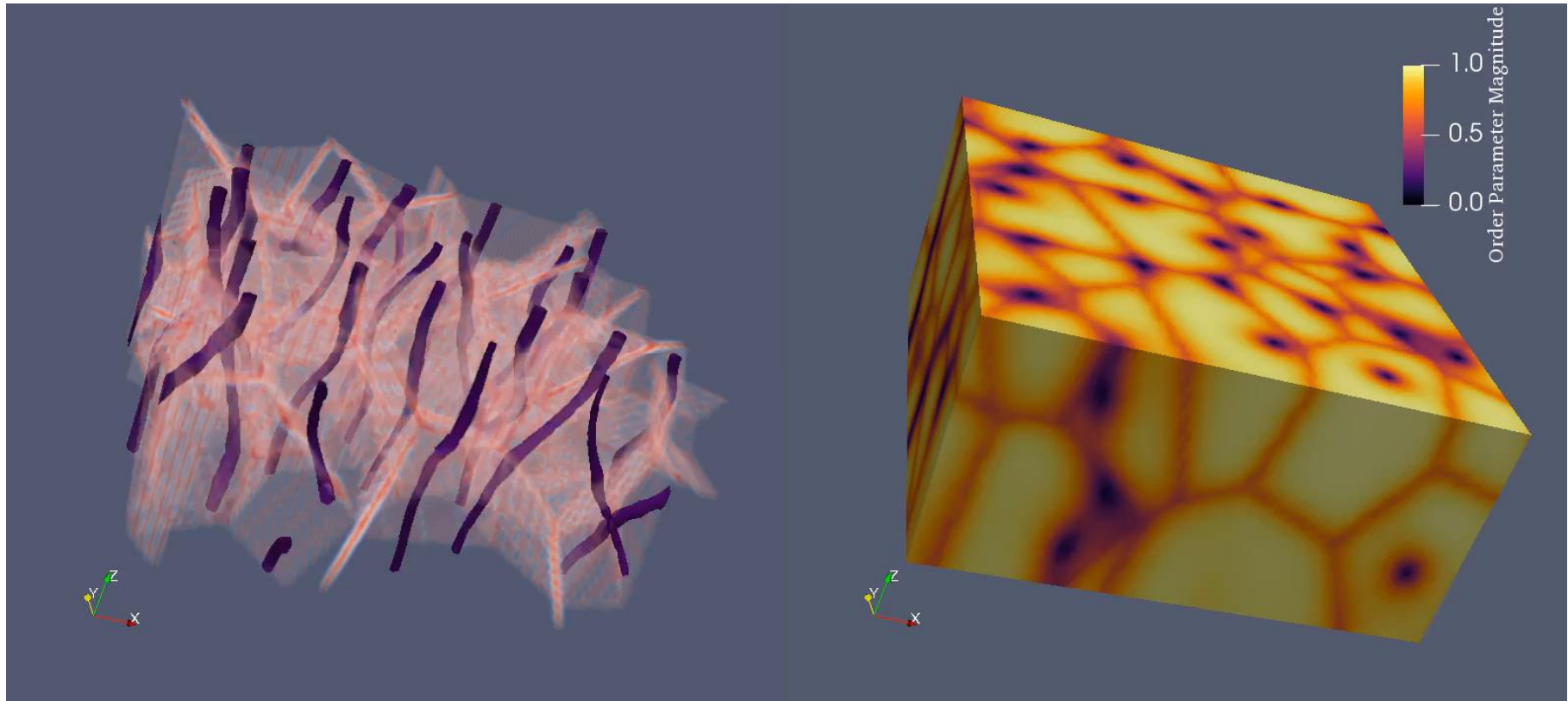
Multigrid speed-up for computational TDGL



Schematic of the 2D computational domain of width w and periodic length l used to model the junction system.

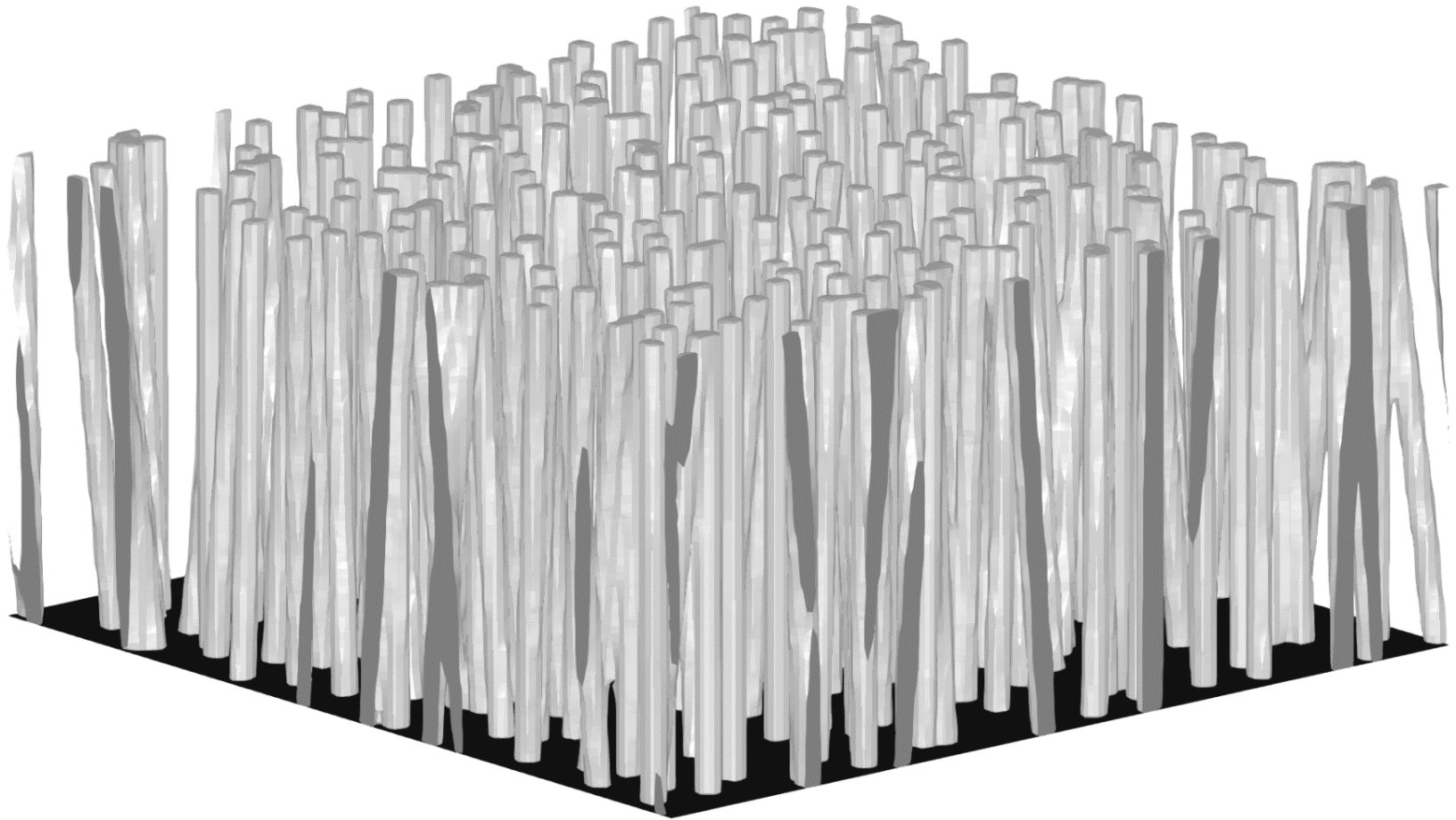
A. I. Blair and D. P. Hampshire [Critical current density of superconducting-normal-superconducting Josephson junctions and polycrystalline superconductors in high magnetic fields](#), Phys. Rev. Research **4**, 023123, 16 May 2022

Flux motion in polycrystalline superconductors – Nb₃Sn



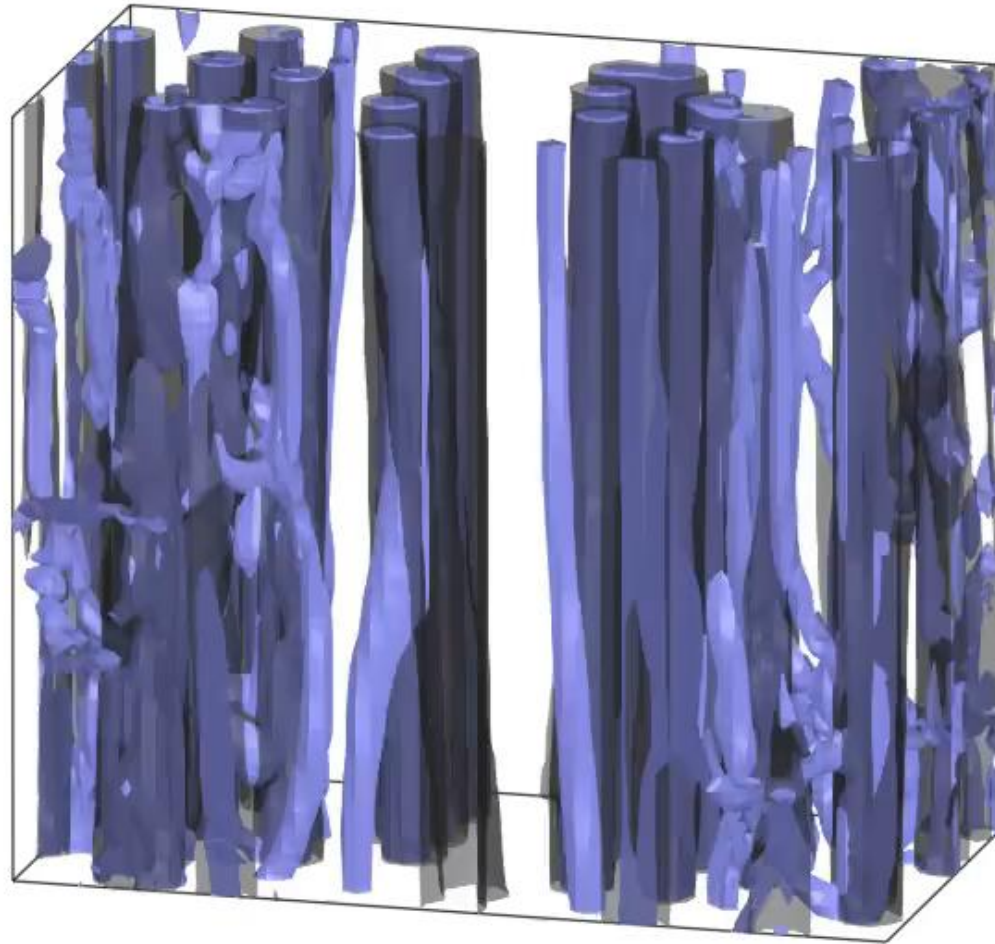
The Critical Current Density of SNS Josephson Junctions and Polycrystalline Superconductors in High Magnetic Fields. [Alex I. Blair](#), [D. P. Hampshire](#) October 2021. [arXiv:2110.02053](#) [pdf]

HTS materials with insulating pins

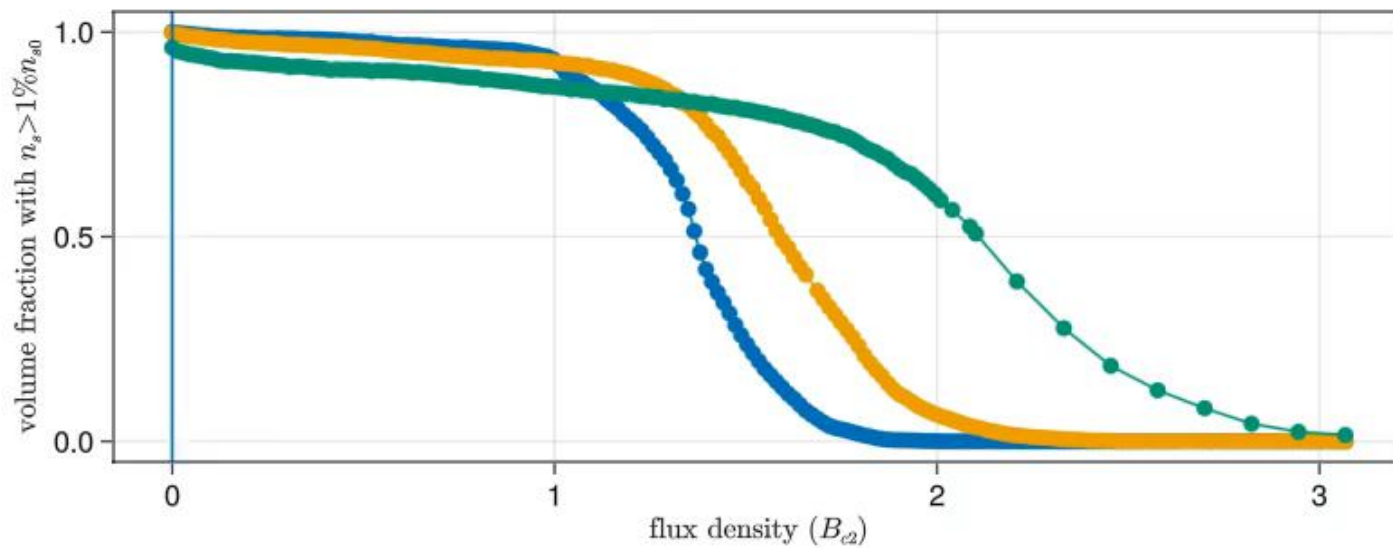
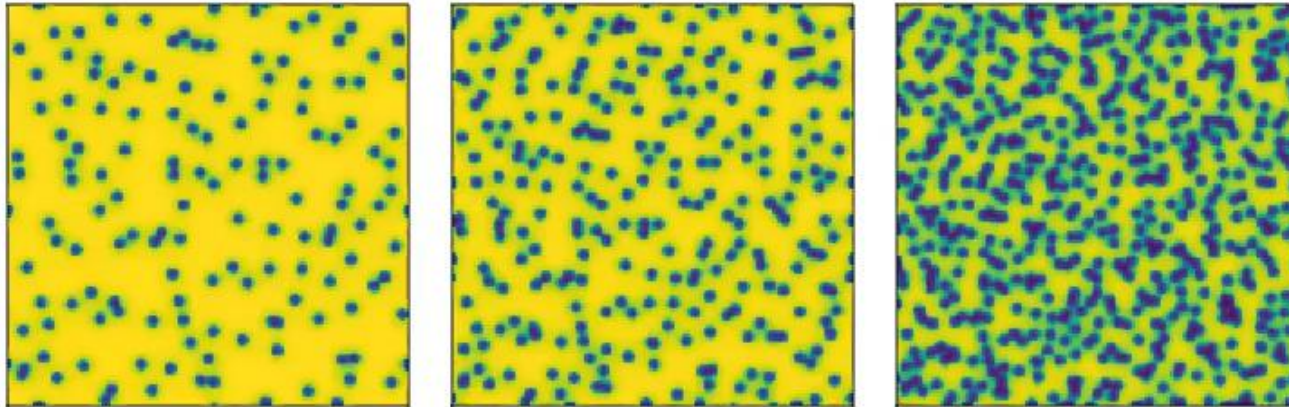


C.W.W. Haddon, A.I. Blair, F. Schoofs, and D.P. Hampshire [Computational Simulations using Time-Dependent Ginzburg-Landau Theory for Nb-Ti-like Microstructures](#) IEEE Transactions on Applied Superconductivity, Article vol. 32, no. 4, p. 5, Jun 2022

HTS materials with insulating pins

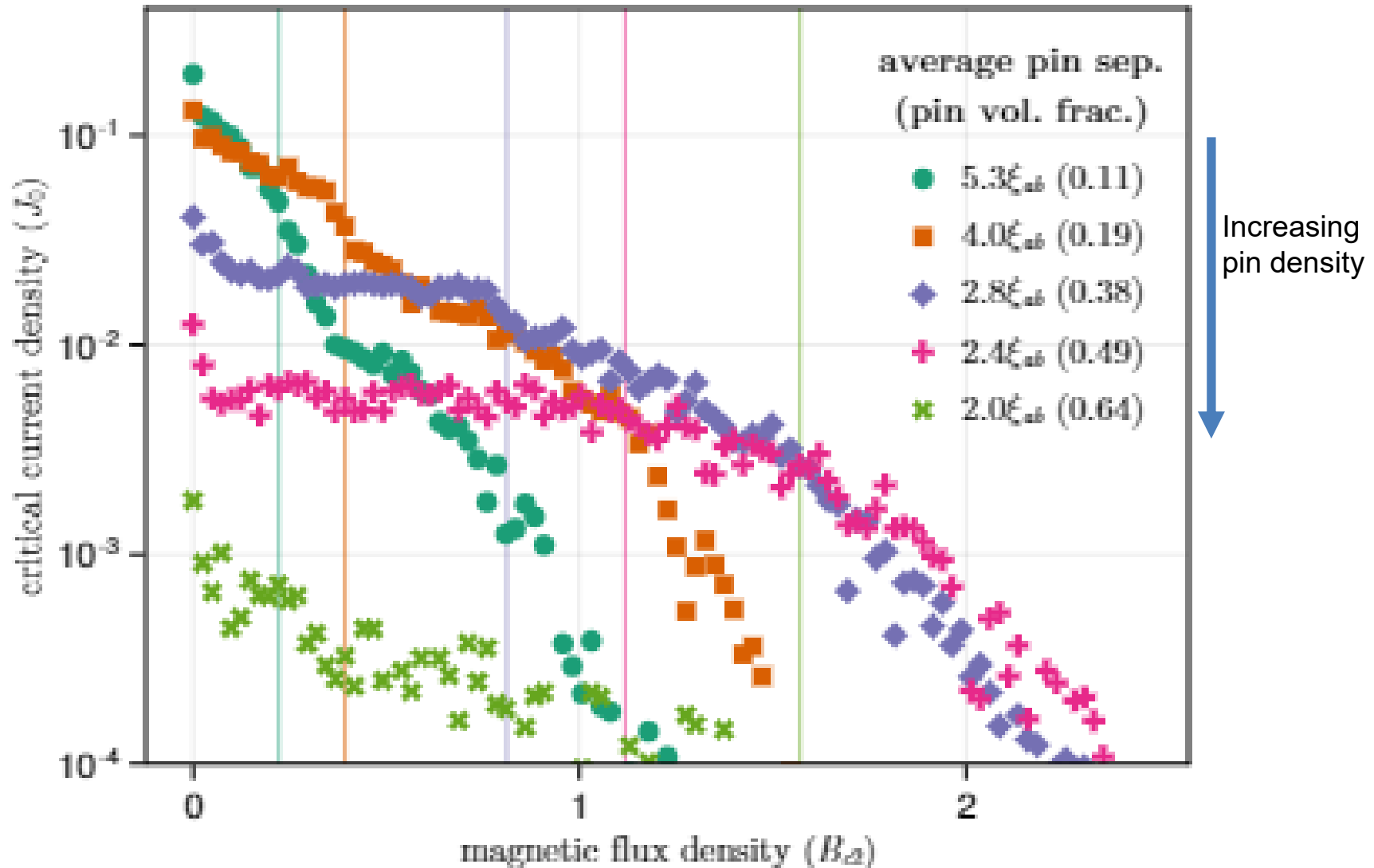


HTS materials – percolation



C. W. W. Haddon and Damian P. Hampshire “[Fast Multigrid Simulations of Pinning in REBCO with Highly Resistive Nanorods](#)” IEEE Transactions on Applied Superconductivity, IEEE Xplore, doi: 10.1109/TASC.2023.3253065.

HTS materials with insulating pins

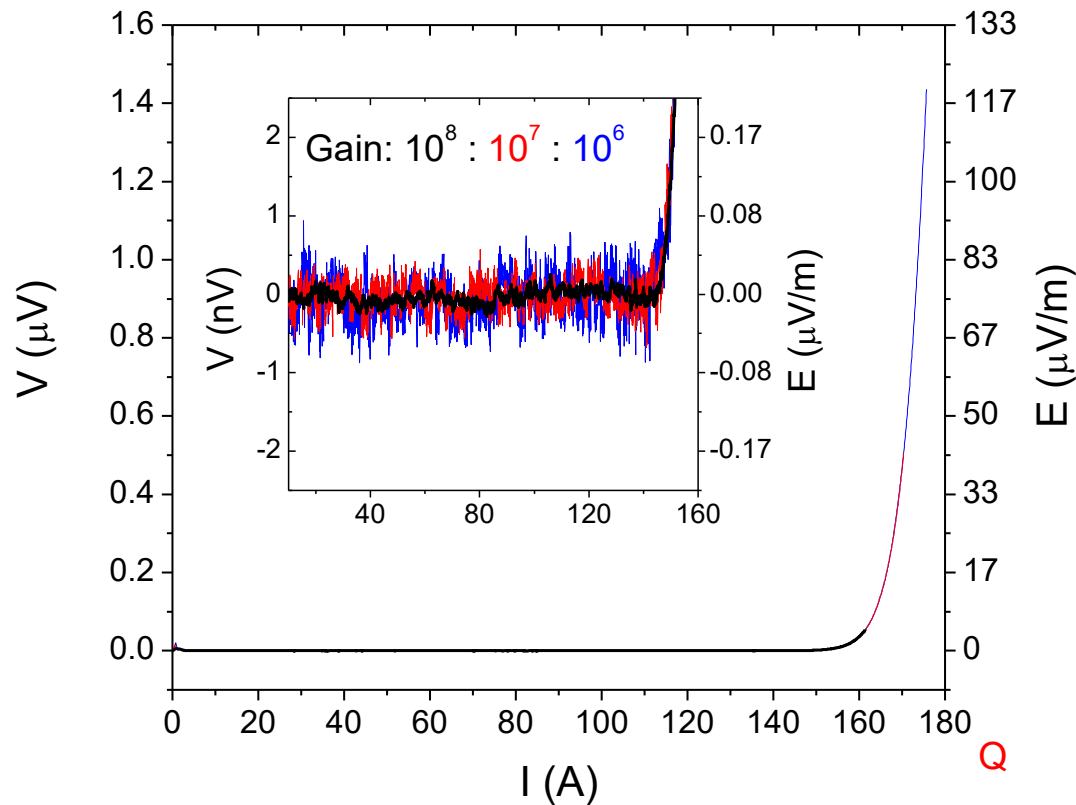


Talk Outline

1. Time-dependent Ginzburg-Landau Theory - Flux pinning visualisation.
 - Irradiation affects J_c (pinning) and B_{c2}
2. Critical current experiments on HTS
3. Avoiding hell in a handcart.
4. Concluding comments.

Critical current density in high magnetic fields

Supercurrents !



$T = 4.2$ K, $B = 7$ T

$V_{\text{theory}} \sim 54$ pV

Measurements are about a factor of 3 above the theoretical Johnson noise limit

Experimental Results for Nb_3Sn and $\text{RE}_1\text{Ba}_2\text{Cu}_3\text{O}_7$

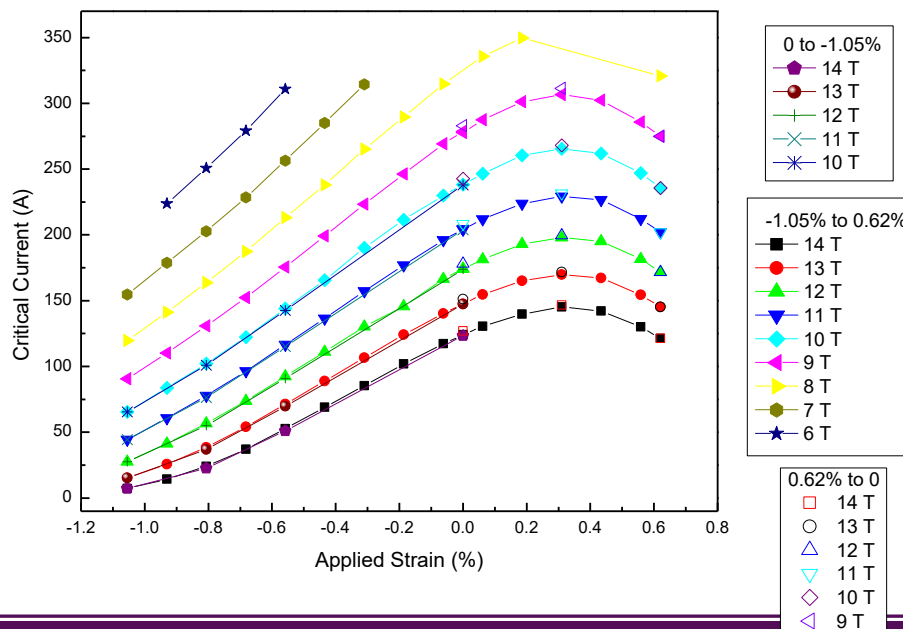
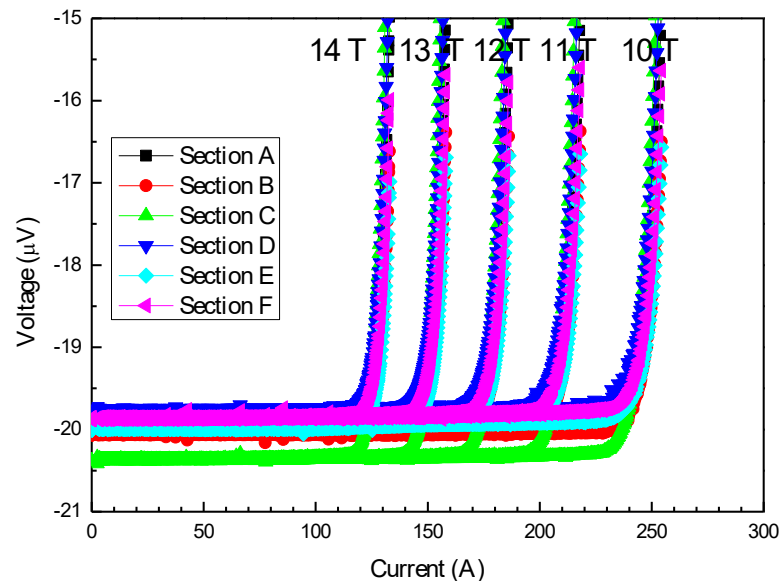
①

Springboard used to apply compressive and tensile strain on tapes

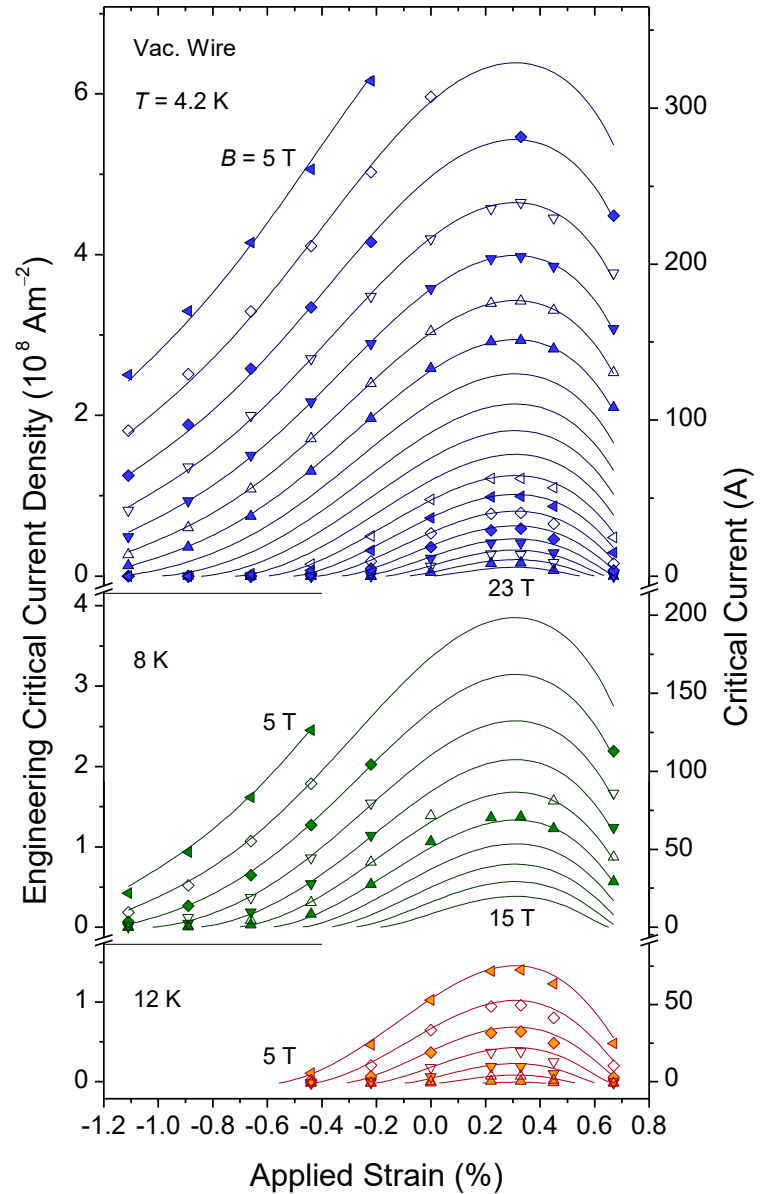
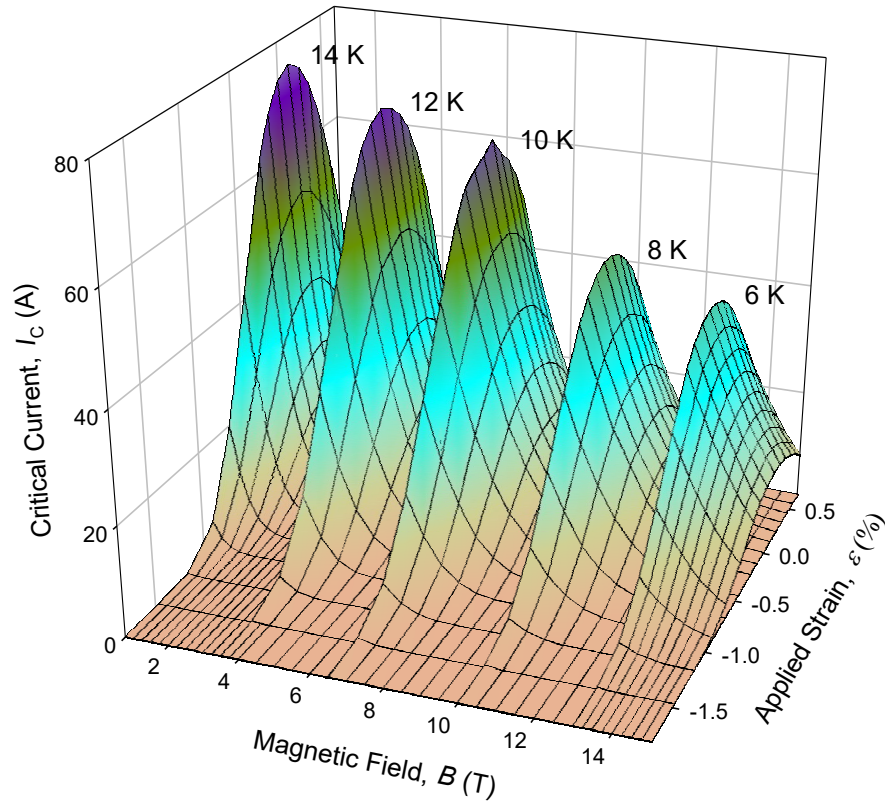


②

Tee-shaped spring for applying compressive and tensile strain to wires

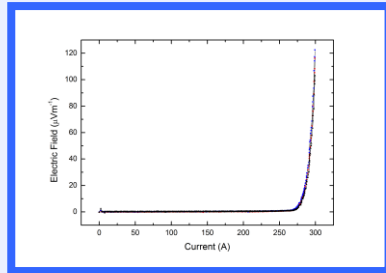


J_C (Magnetic field B , Temperature T , Strain ε) - Nb_3Sn



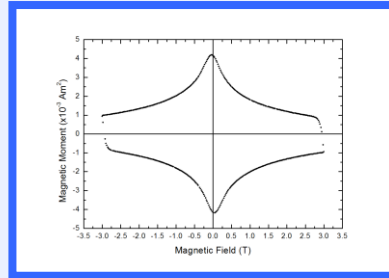
Durham's Role in the ITER project – Engineering approach ¹⁶

Critical Current, $I_c > 190$ A



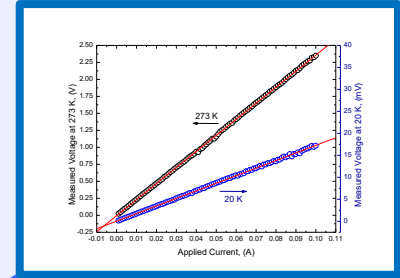
1000

Hysteresis < 500 mJ/cm³



500

Residual Resistivity Ratio > 100



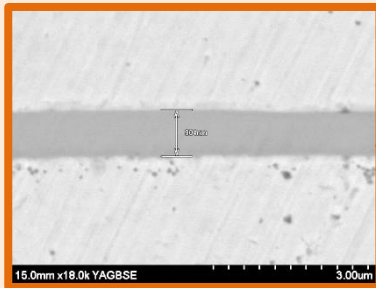
1000

Cryogenic measurements (down to -269 °C)

Cryogenic measurements (down to -269 °C)

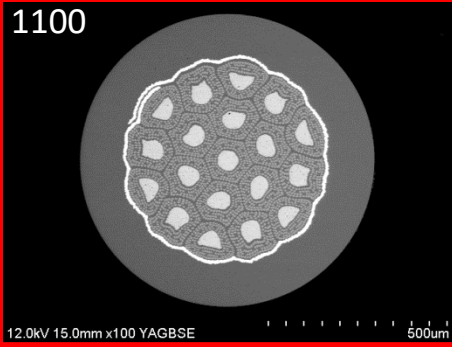
Room temperature measurements

Room temperature measurements



1000

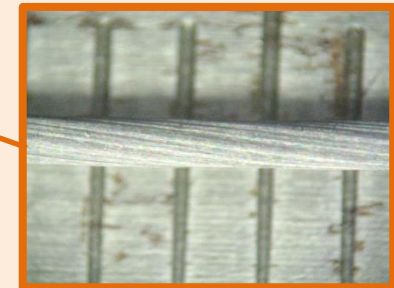
Chromium Plating Thickness, 1 to 2 μm



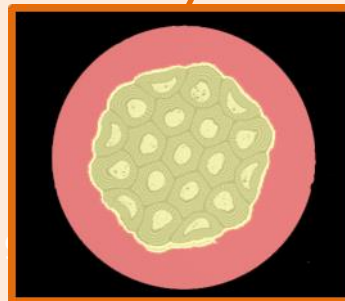
1100

1000

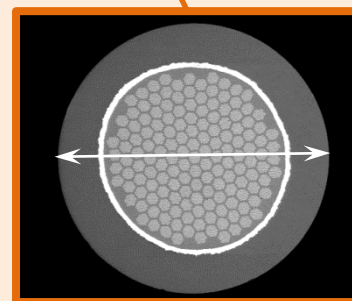
1000



Twist Pitch 15 ± 2 mm



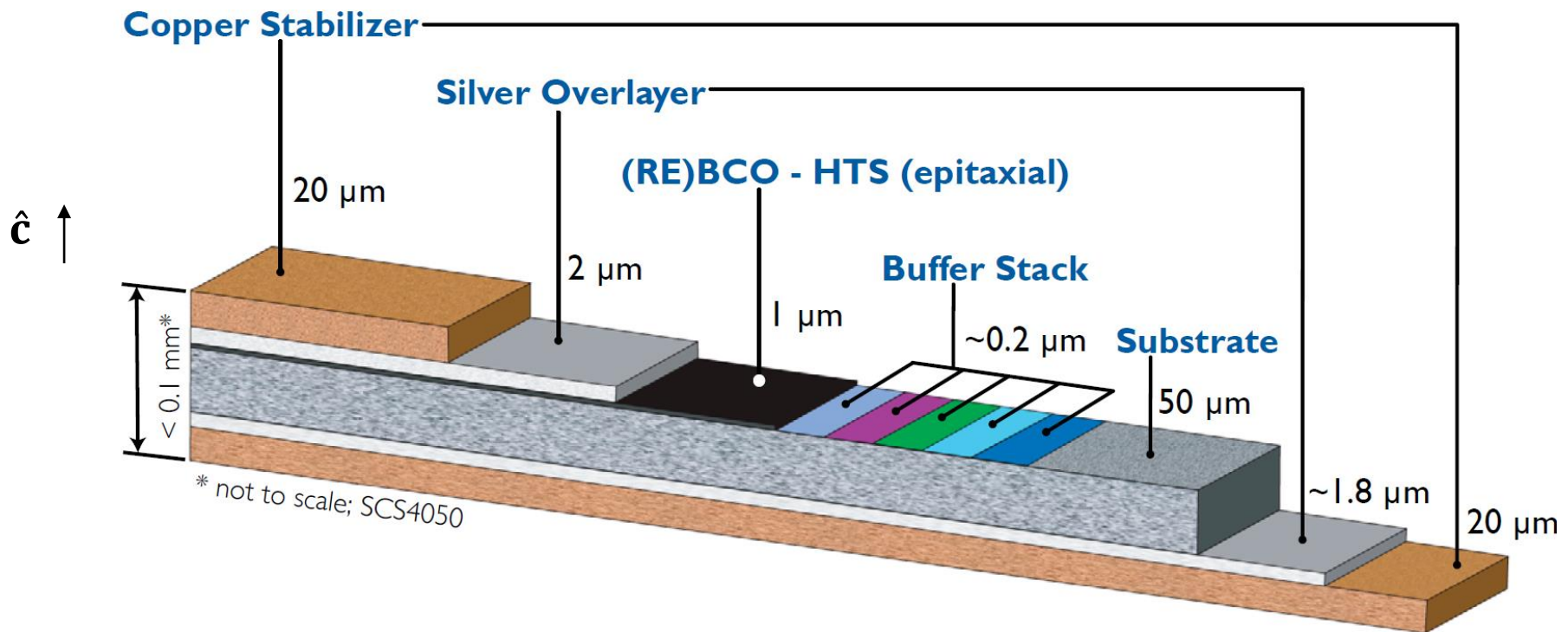
Cu-non-Cu Ratio, 1.0 ± 0.1



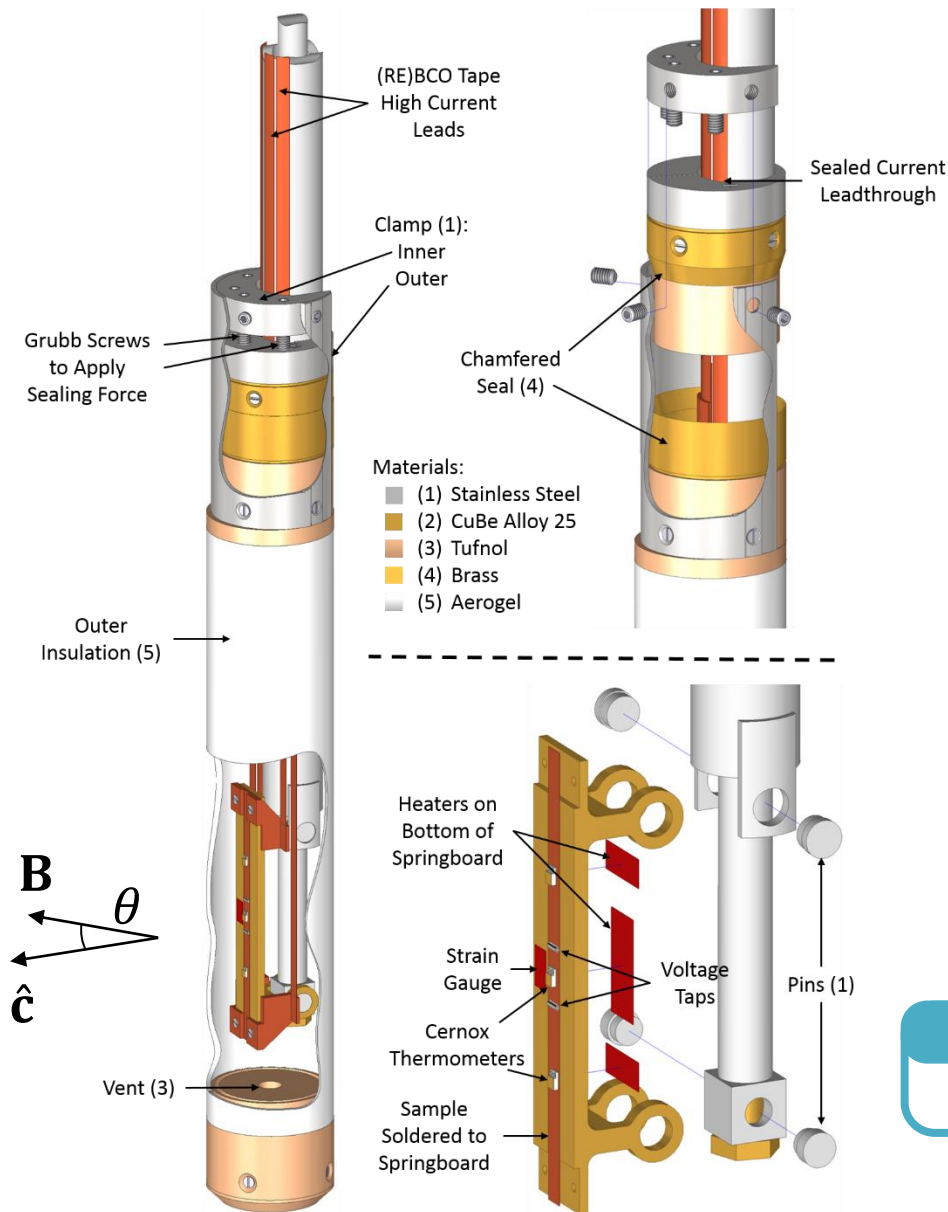
Diameter, 0.820 ± 0.005 mm

The HTS Samples

4 mm wide SuperPower Tape (AP and non-AP): $(\text{RE})\text{Ba}_2\text{C}_3\text{O}_{7-\delta}$ (RE = Rare Earth), $T_c \approx 90 \text{ K}$



Variable strain experimental Setup



Applied Strain

$$-1.0 \% \lesssim \varepsilon \lesssim +0.5 \%$$

Temperature

$$4.2 \text{ K} \leq T \leq 150 \text{ K}$$

Current

$$I \leq 250 \text{ A}$$

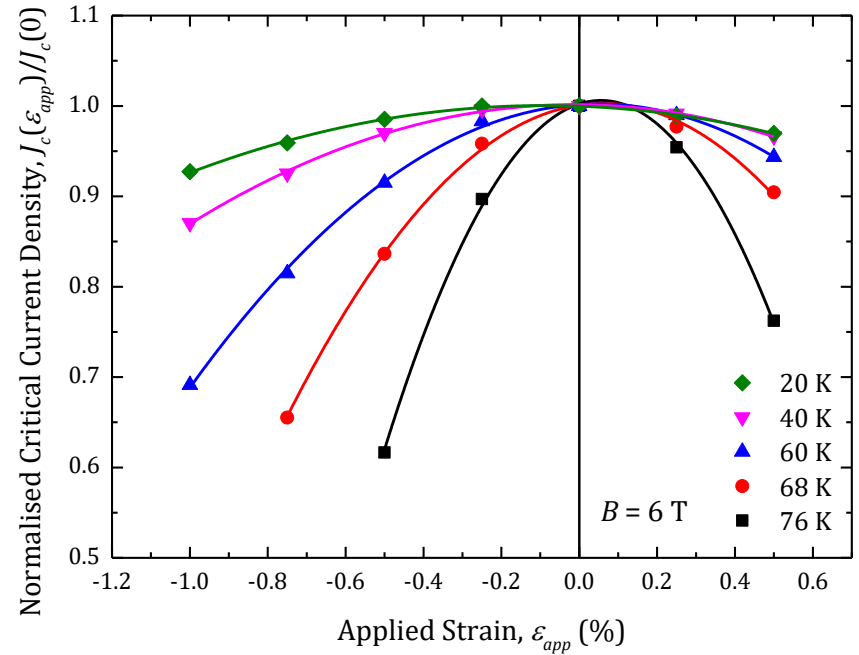
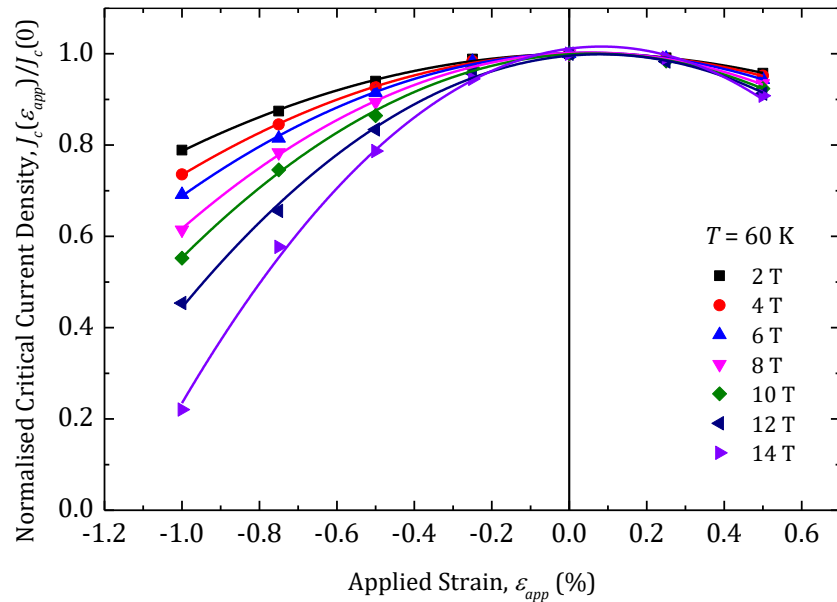
Angle

$$0^\circ \leq \theta \leq 360^\circ$$

Magnetic Field

$$B \leq 15 \text{ T} - 40 \text{ mm Split} - \text{pair magnet}$$

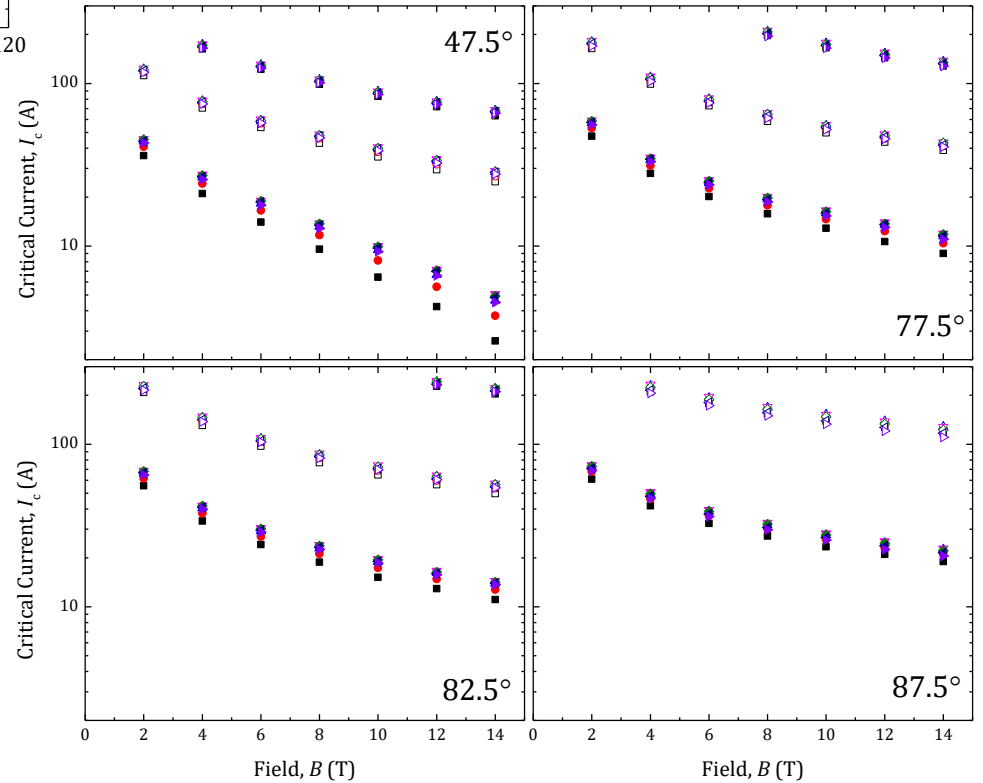
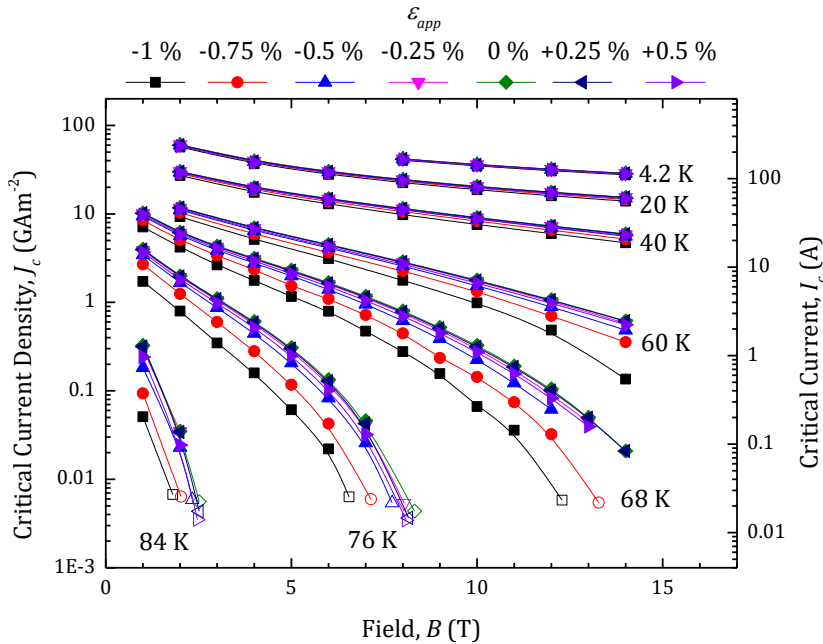
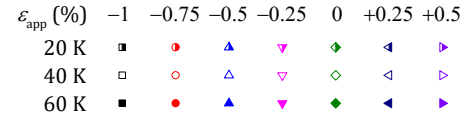
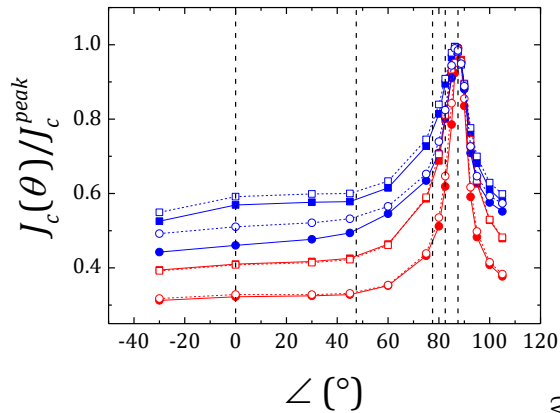
Parabolic Behaviour of $J_c(\varepsilon_{app})$



Parabolic fits to variable strain data

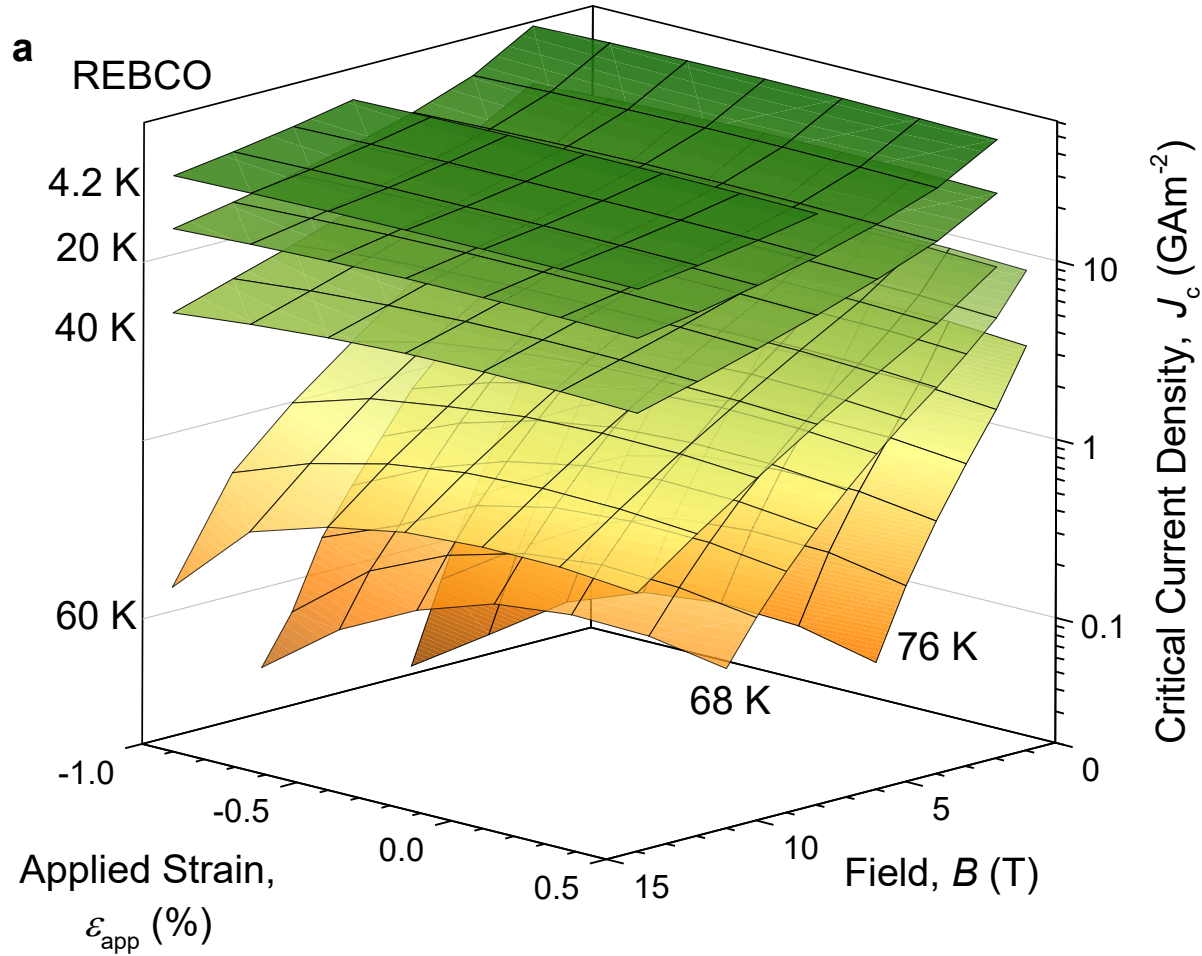
$$\frac{J_c(\varepsilon_{app})}{J_c(0)} = 1 - \beta(\varepsilon_{app} - \varepsilon_{peak})^2 + \beta\varepsilon_{peak}^2$$

Extensive
critical current
data taken at
selected angles

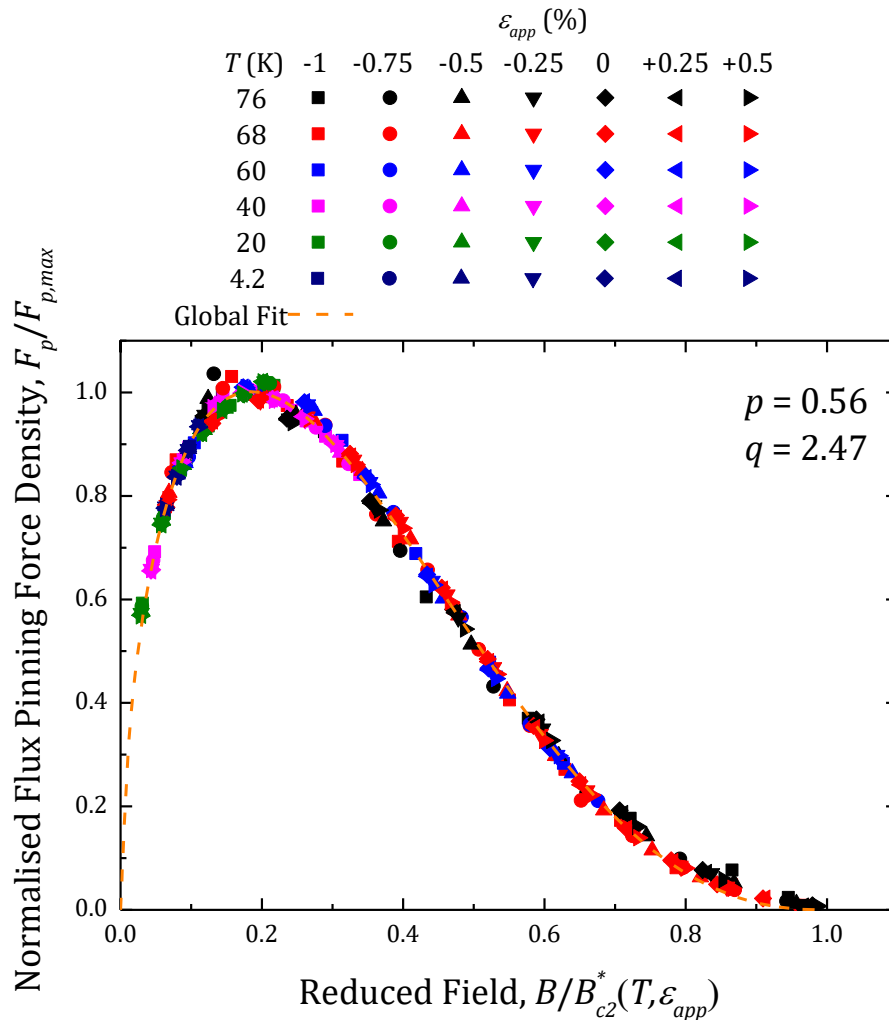


High quality critical current data over a large region of parameter space

Experimental J_c data for REBCO

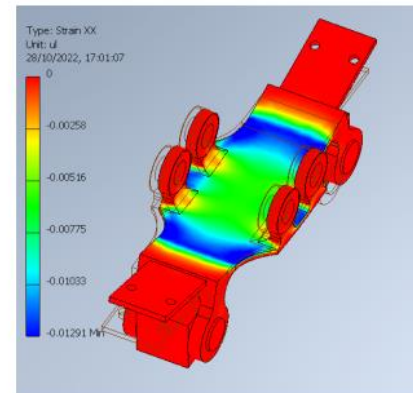


$$F_p(T, B(\theta = 0^\circ), \varepsilon_{app})$$



Flux pinning curve scales well with temperature and strain

$$F_p = J_c B = C \left(\frac{B}{B_{c2}} \right)^p \left(1 - \frac{B}{B_{c2}} \right)^q$$

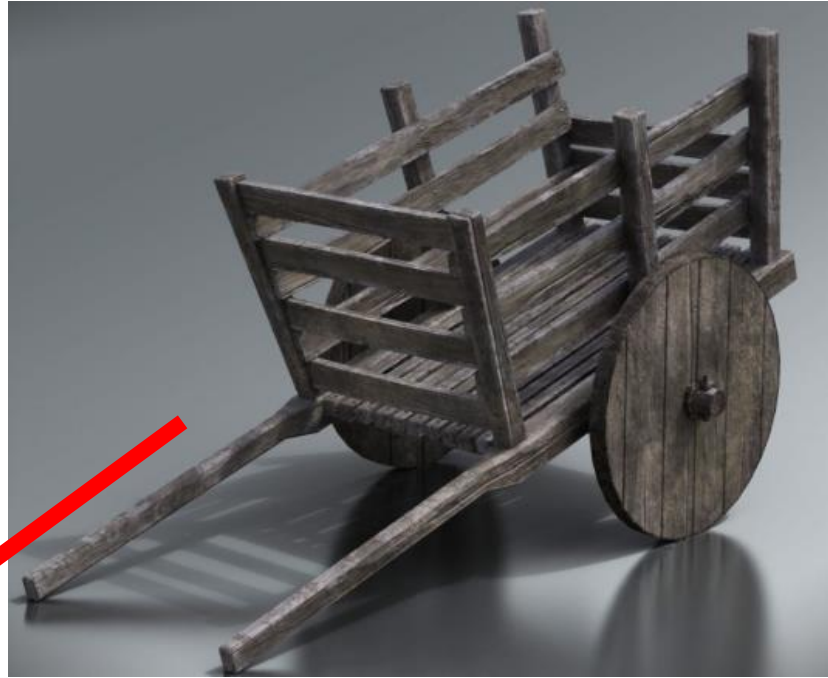


2D measurements

Talk Outline

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2. Critical current experiments on HTS
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Avoiding hell in a hand-cart

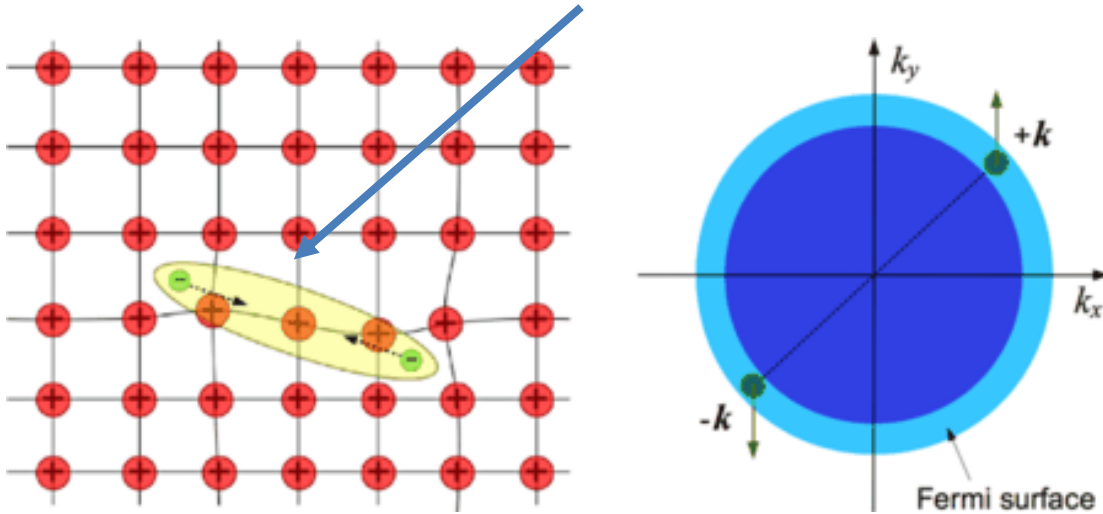


To hell

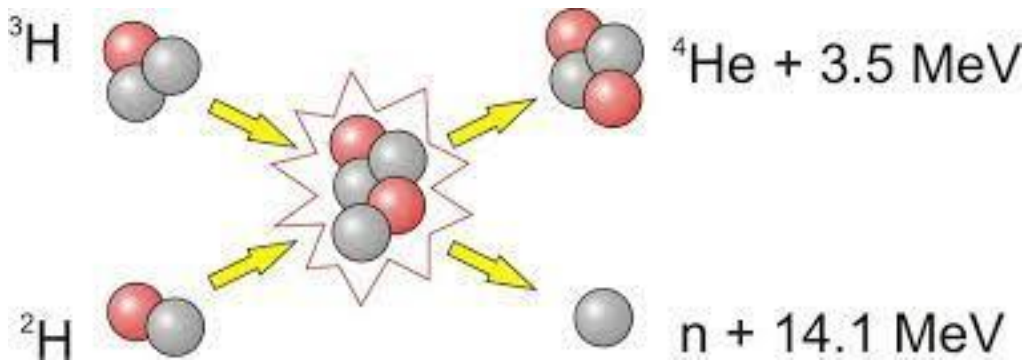
Turn the D-T plasma on
and simultaneously turn the
superconducting magnets off

Nine orders of magnitude energy range.

Beautiful fragile Cooper pair

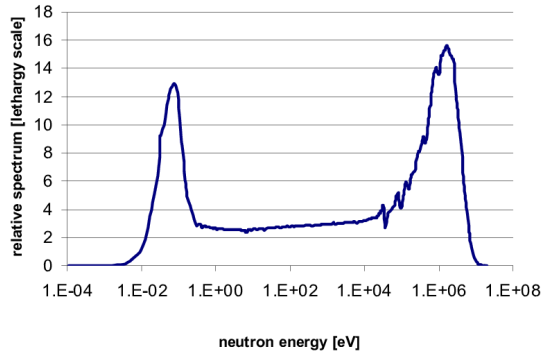


Cooper pair
 $E \sim 20 \text{ meV}$
 $d_0 \sim 2 \text{ nm}$
 $T \sim 10 \text{ ns}$



Neutron energy
 $\sim 14 \text{ MeV}$

Electromagnetic Spectrum

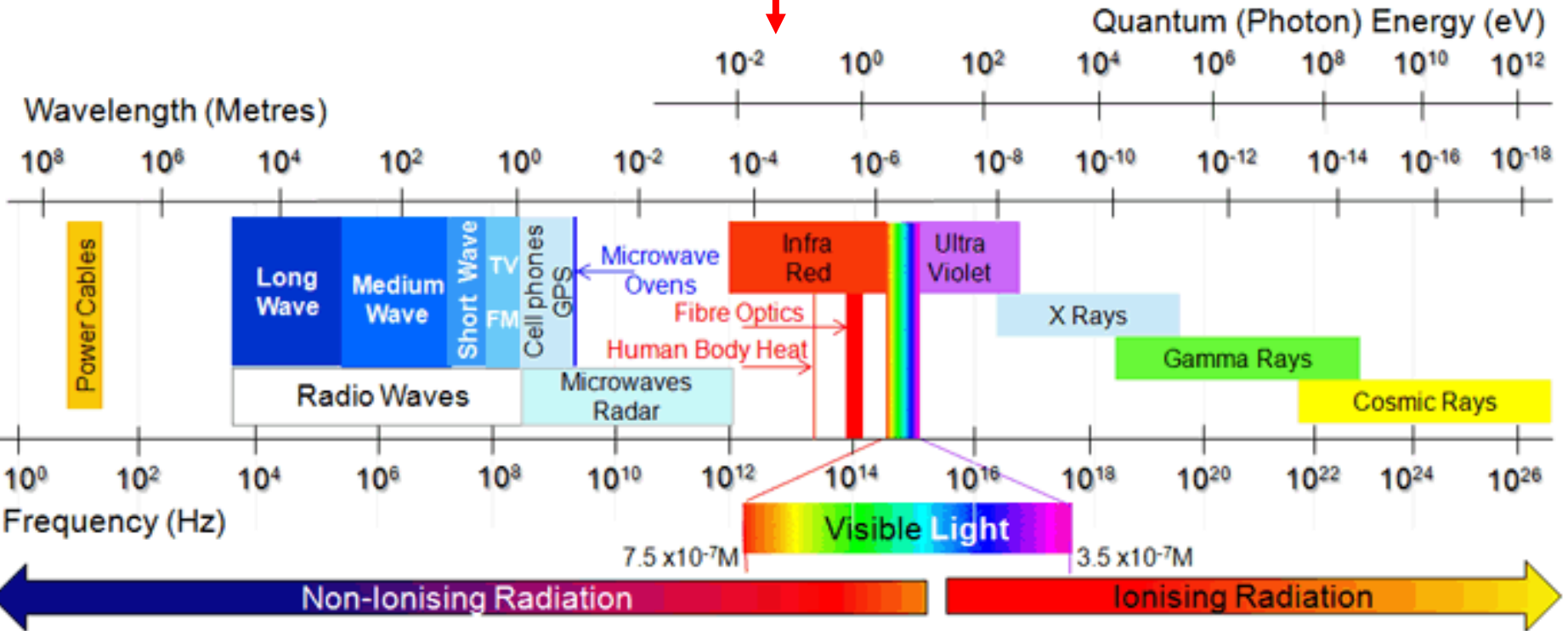


Triga III spectrum

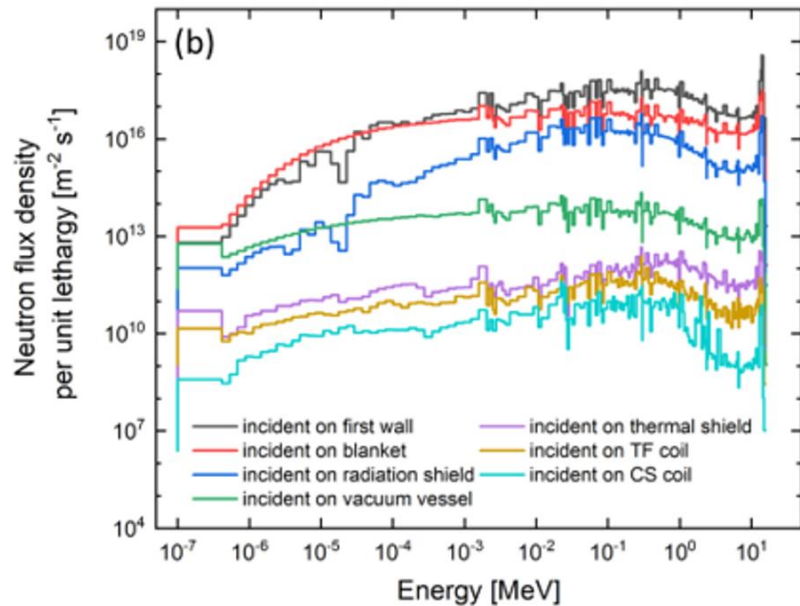
9 Orders of Magnitude !!

Fusion D-T energy ~ 14 MeV

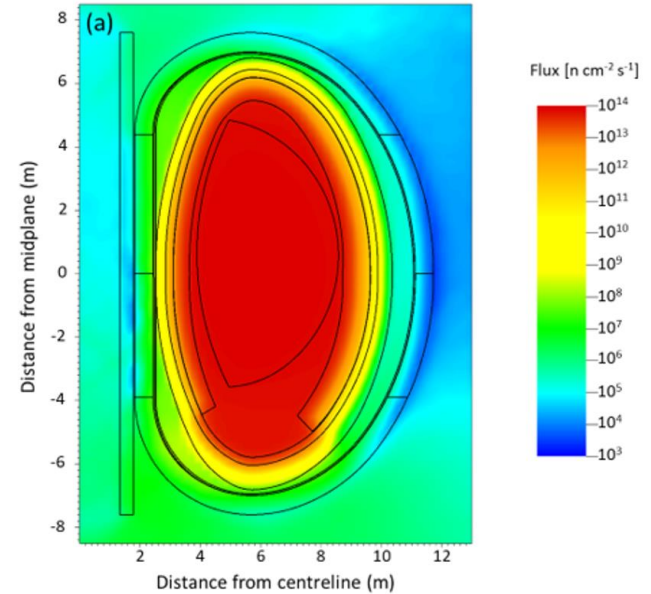
Cooper pair energy ~ 20 meV
 Skin depth ~ 1/2 micron !



Neutron flux in a tokamak

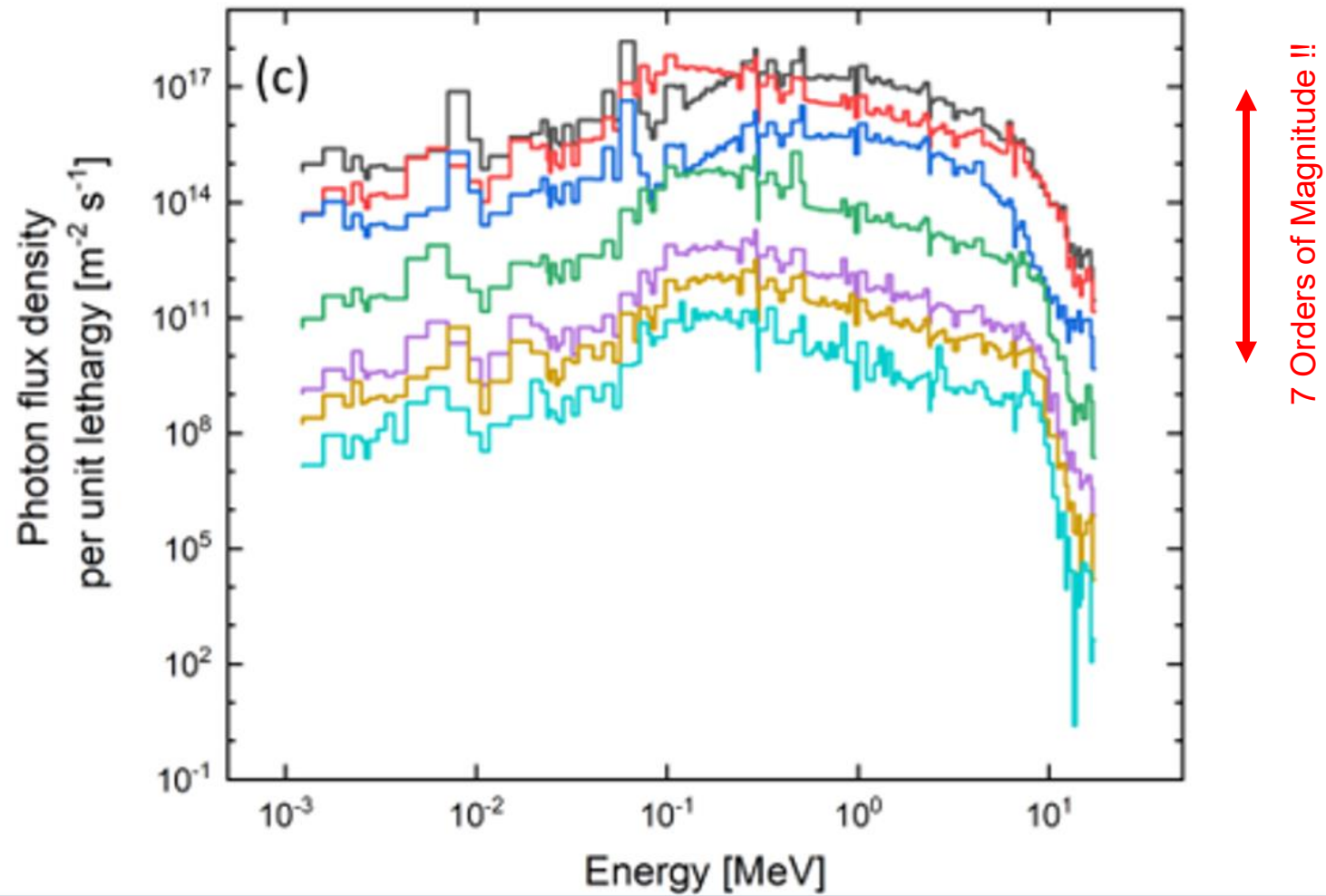


7 Orders of Magnitude !!



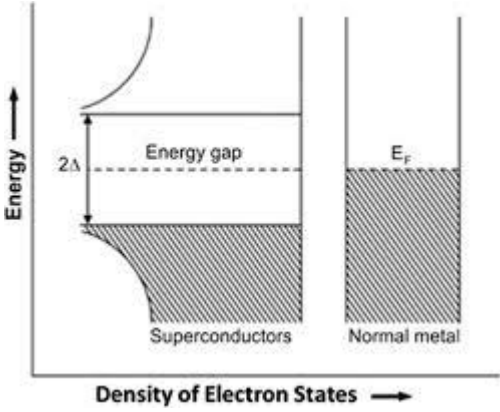
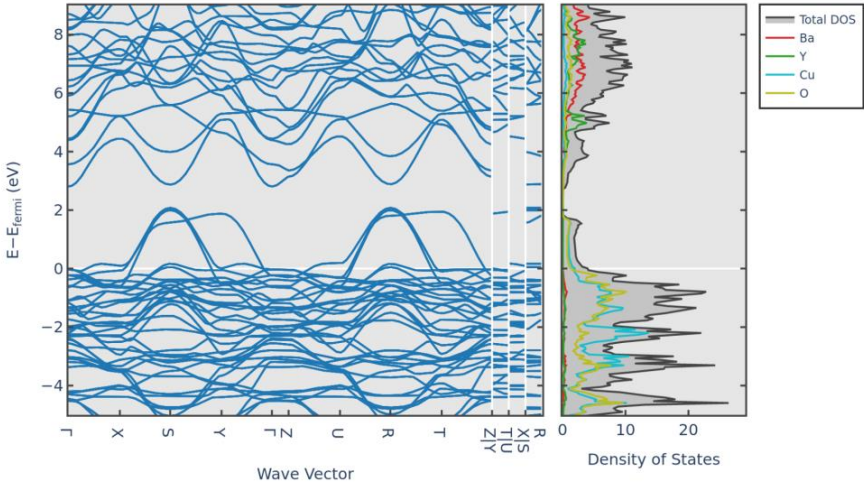
Chislett-McDonald S, Hampshire D P, et al. Training and Upgrading Tokamak Power Plants with Remountable Superconducting Magnets. Los Alamos archive: <https://arxiv.org/abs/2205.04441v1> (2022)

Photon flux in a tokamak

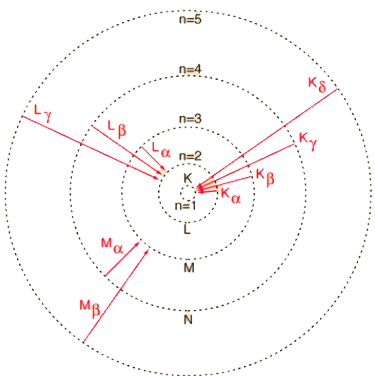


Charateristic energies in materials

Conduction electrons \sim eV

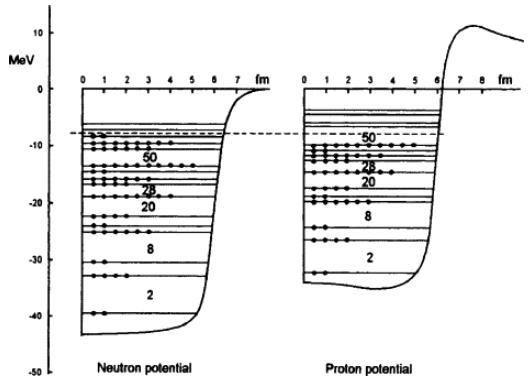


Fragile Cooper pair \sim 20 meV



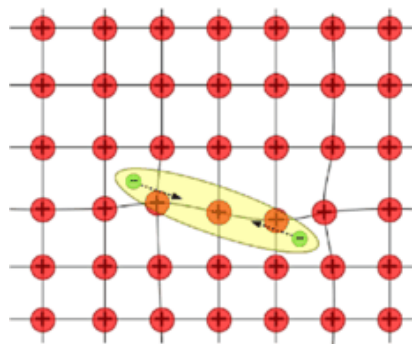
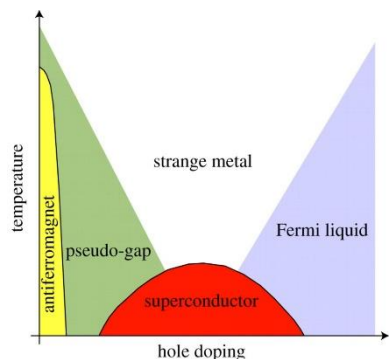
Core electrons \sim keV

Nuclear structure \sim MeV



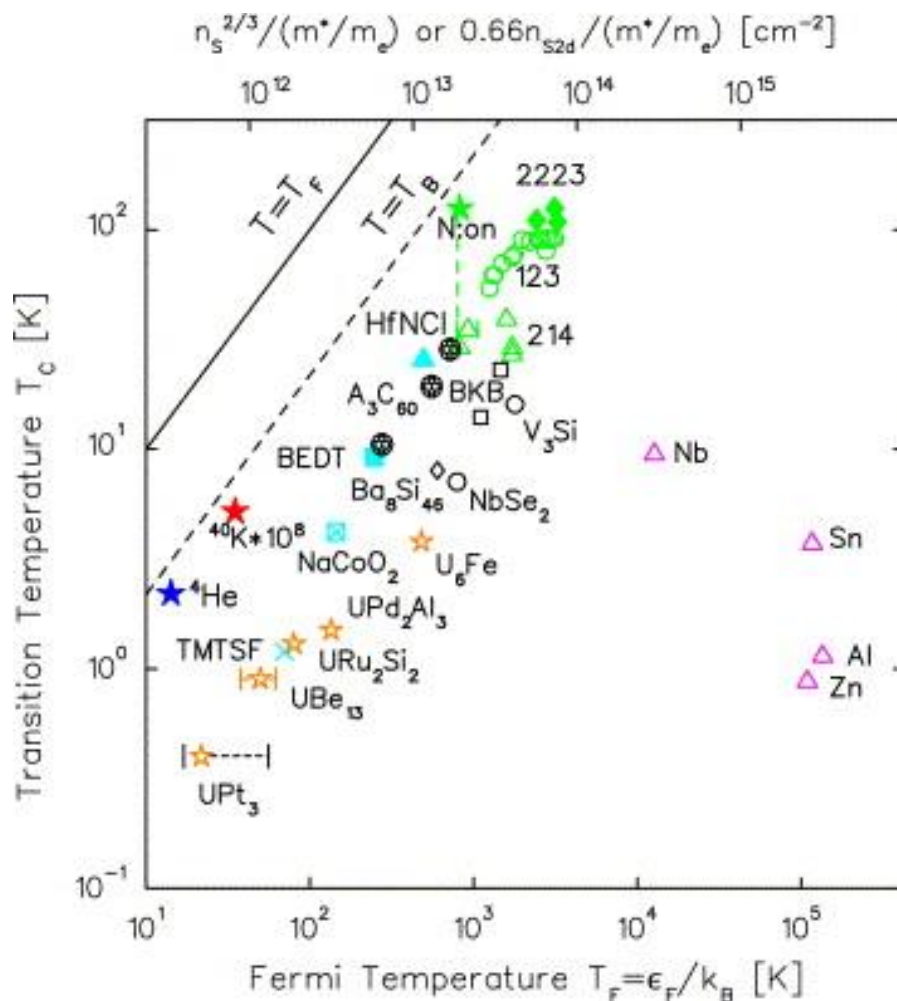
Unconventional Superconductivity ??

- The microscopic mechanism



- Phonons
- Spin waves
- Antiferromagnetic magnons
- Bose-Einstein condensate
-

- Low carrier density
- Reduced dimensionality
- d-wave
- Metal-Insulator transition
-



Dynamic equilibrium under a plasma flux

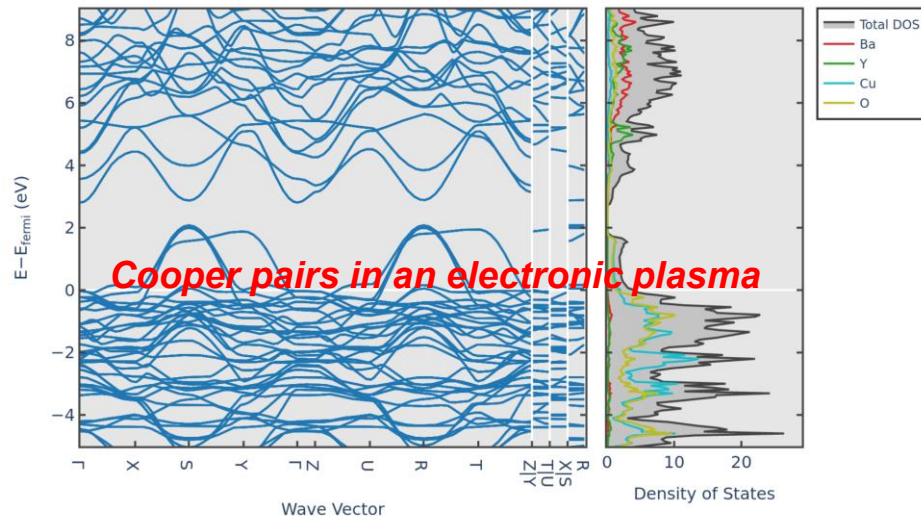
Whistling past in (real) space

Neutrons and photons with energies from MeV to meV.

Cascades of ions and defects.

Cascades of electrons.

- In dynamic equilibrium on time-scales from ns to years.



The k-space or E-space environment.

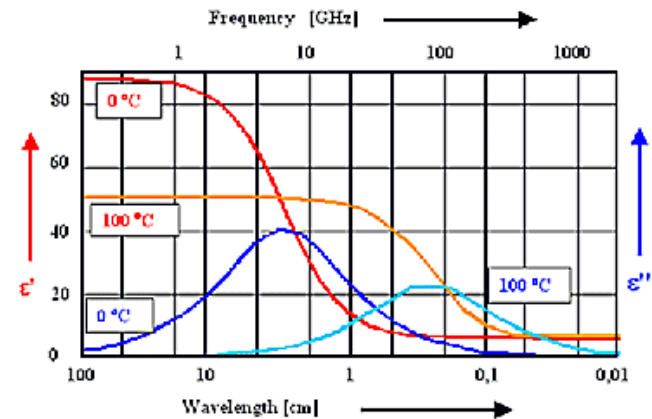
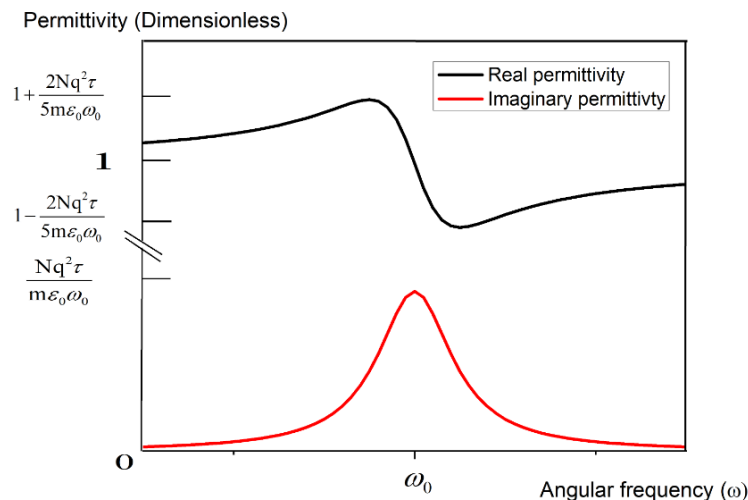
Cascades of electrons falling through energy levels from free electrons, through conduction electron levels to the core electron levels.

Disturbed phonon and magnons structures.

- All changing on time-scales upwards from ns.

Simple Harmonic Oscillator

"There are only two problems in physics: the simple harmonic oscillator problem and turning every other problem into the simple harmonic oscillator problem"



The Permittivity of a dielectric as a function of angular frequency

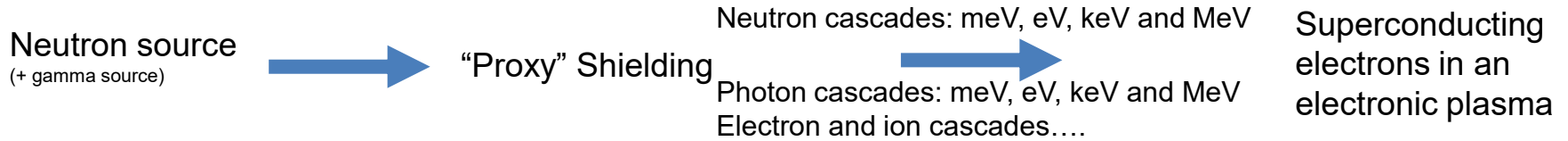
Computation:

Lattice: Calculations + measurements + oxygen annealing.

Electronic structure: DFT including correlations.

“Challenges: ‘Time-scale of nanoseconds, lattice chaos and electronic plasma’”

Superconducting-electronic-plasma ~ 10 ms (or ~ 10 s) experiment



Two rules for experiment for the electronic plasma:

- The flux of neutrons and photons must be within a factor of 10 of that in the tokamak across the entire energy range from meV to MeV (Ic measurements are $\sim 1\%$ accurate).
- The irradiated superconductor must be irradiated and measured at cryogenic temperatures, under high field (and angle) at strain **under operational conditions**.

For experimentalists:

- Following some beautiful data at IREF23, let's (avoid contradictory Jc data under irradiation) try to get the thermometer as close as possible/in good thermal contact with the sample.

Financial risk + reputational risk! Cost of EDF's new UK nuclear project rises to \$40 billion:

<https://www.reuters.com/business/energy/cost-edfs-new-uk-nuclear-project-soars-40-bln-2023-02-20/>

Concluding Comments

TDGL shows J_c and B_{c2} changes with irradiation

$J_c(B, T, \theta, \epsilon)$ for HTS is broadly understood
- there is still headroom for improvement in magnitude.

Measurements of J_c are demanding and time consuming.

We need J_c measurements under ***operational conditions*** including photon/neutron flux with energies over 9 orders of magnitude.

